

3 DESIGNS

n	Cardinality C												
n	2n+1	2n+3	2n+5	2n+7	2n+9	2n+11	2n+13	2n+15	2n+17	2n+19	2n+21	2n+23	2n+25
3	7*	9	11										
4	9*	11											
5	11*	13	15										
6	13*	15											
7	15*	17○	19										
8	17*	19◇	21										
9	19*	21•	23										
10	21*	23•	25										
11	23*	25*	27	29									
12	25*	27*	29○	31									
13	27*	29*	31◇	33									
14	29*	31*	33◇	35									
15	31*	33*	35•	37	39								
16	33*	35*	37•	39○	41								
17	35*	37*	39•	41○	43								
18	37*	39*	41•	43◇	45								
19	39*	41*	43*	45◇	47	49							
20	41*	43*	45*	47◇	49	51							
21	43*	45*	47*	49•	51○	53							
22	45*	47*	49*	51•	53○	55							
23	47*	49*	51*	53•	55◇	57	59						
24	49*	51*	53*	55•	57◇	59	61						
25	51*	53*	55*	57•	59◇	61	63						
26	53*	55*	57*	59•	61◇	63○	65						
27	55*	57*	59*	61*	63•	65○	67	69					
28	57*	59*	61*	63*	65•	67◇	69	71					
29	59*	61*	63*	65*	67•	69◇	71	73					
30	61*	63*	65*	67*	69•	71◇	73	75					

Table 3 designs

31	63*	65*	67*	69*	71•	73◇	75○	77	79				
32	65*	67*	69*	71*	73•	75•	77○	79	81				
33	67*	69*	71*	73*	75•	77•	79◇	81	83				
34	69*	71*	73*	75*	77•	79•	81◇	83	85				
35	71*	73*	75*	77*	79*	81•	83◇	85○	87	89			
36	73*	75*	77*	79*	81*	83•	85◇	87○	89	91			
37	75*	77*	79*	81*	83*	85•	87◇	89○	91	93			
38	77*	79*	81*	83*	85*	87•	89•	91◇	93	95			
39	79*	81*	83*	85*	87*	89•	91•	93◇	95	97	99		
40	81*	83*	85*	87*	89*	91•	93•	95◇	97○	99	101		
41	83*	85*	87*	89*	91*	93•	95•	97◇	99○	101	103		
42	85*	87*	89*	91*	93*	95*	97•	99◇	101○	103	105		
43	87*	89*	91*	93*	95*	97*	99•	101◇	103◇	105	107	109	
44	89*	91*	93*	95*	97*	99*	101•	103•	105◇	107	109	111	
45	91*	93*	95*	97*	99*	101*	103•	105•	107◇	109○	111	113	
46	93*	95*	97*	99*	101*	103*	105•	107•	109◇	111○	113	115	
47	95*	97*	99*	101*	103*	105*	107•	109•	111◇	113○	115	117	119
48	97*	99*	101*	103*	105*	107*	109•	111•	113◇	115◇	117	119	121
49	99*	101*	103*	105*	107*	109*	111•	113•	115◇	117◇	119○	121	123
50	101*	103*	105*	107*	109*	111*	113*	115•	117•	119◇	121○	123	125

KEY :

|m - design with cardinality $|C| \geq m$ exists by [1];

m* - nonexistence by [2] and [3];

m• - nonexistence by [4];

m◇ - nonexistence by [5] and [6];

m○ - nonexistence by [7] and [8];

m - open case

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